Review

Recent Advances in Brillouin Optical Correlation-Domain Reflectometry

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Featured Application: Structural health monitoring.

Abstract: Distributed fiber-optic sensing based on Brillouin scattering has been extensively studied and many configurations have been developed so far. In this paper, we review the recent advances in Brillouin optical correlation-domain reflectometry (BOCDR), which is known as a unique technique with intrinsic single-end accessibility, high spatial resolution, and cost efficiency. We briefly discuss the advantages and disadvantages of BOCDR over other Brillouin-based distributed sensing techniques, and present the fundamental principle and properties of BOCDR with some special schemes for enhancing the performance. We also describe the recent development of a high-speed configuration of BOCDR (slope-assisted BOCDR), which offers a beyond-nominal-resolution detectability. The paper is summarized with some future prospects.

Keywords: Brillouin scattering; optical fiber sensing; optical correlation-domain reflectometry; distributed sensing; strain sensing; temperature sensing; nonlinear optics; structural health monitoring

1. Introduction

Since the Brillouin frequency shift (BFS) in optical fibers was found to be dependent on applied strain and ambient temperature [1–4], extensive research has been conducted to exploit Brillouin scattering to develop distributed fiber-optic sensors. The first demonstrations were performed by time-of-flight techniques; they are called Brillouin optical time-domain analysis (BOTDA) [5] and Brillouin optical time-domain reflectometry (BOTDR) [6]. In both techniques, optical pulses are injected into fibers under test (FUTs), and by measuring the time until the reflected signals are returned, the locations in the FUTs can be derived. In BOTDR, optical pulses are injected into only one end of the FUT, and they are partially returned via spontaneous Brillouin scattering. In contrast, in BOTDA, a continuous wave (probe) is injected into the other end of the FUTs in addition to the optical pulses (pump). The frequency of the probe light is downshifted by the BFS in advance, and then the pump and probe lights interact with each other, inducing stimulated Brillouin scattering (SBS). As SBS is much stronger than spontaneous Brillouin scattering, the signal-to-noise ratio (SNR) of BOTDA is much higher than that of BOTDR, leading to a shorter measurement time because of the reduced averaging count. However, unlike BOTDR with single-end accessibility, the two-end-access nature of BOTDA is not beneficial to users, because the degree of freedom in deploying the fiber is lowered and the measurement can no longer be continued if the fiber has one breakage point. Thus, BOTDR and BOTDA are in a trade-off relationship. The spatial resolution of these time-domain techniques is determined by the pulse width of the pump light. The basic limitation of the pulse width is known to be approximately 10 ns (corresponding to the spatial resolution of ~1 m) because of the spectral broadening of the Brillouin gain spectrum (BGS) and reduced accuracy of BFS detection [7]. It is
noteworthy that the performance including the spatial resolution has been drastically enhanced with various schemes both in BOTDR [8–11] and in BOTDA [12–20]; refer to each reference for the details. Researchers have also developed Brillouin optical frequency-domain analysis (BOFDA) [21–23] and Brillouin optical frequency-domain reflectometry (BOFDR) [24], which seem to suffer from their relatively slow operation speed because of the large amount of calculation; their details are also out of the scope of this paper.

The other configurations of Brillouin-based distributed fiber-optic sensors are Brillouin optical correlation-domain analysis (BOCDA) [25–35] and Brillouin optical correlation-domain reflectometry (BOCDR) [36,37]. These techniques utilize not optical pulses but frequency-modulated continuous waves to achieve distributed measurements and thus possess so-called random accessibility to sensing points and high spatial resolution without specially configured implementations. BOCDA is a two-end-access system, which operates based on stimulated Brillouin scattering and thus has a relatively high SNR. The details of BOCDA will be fully described in other papers of this Special Issue. Although the SNR of BOCDR is lower than that of BOCDA, its single-end accessibility is beneficial to users as the degree of freedom in embedding the fiber is higher and distributed sensing can be continued even when the fiber is broken at a certain point during the measurement.

In this paper, we review the fundamentals and recent advances in BOCDR, with an emphasis on its high-speed configuration. In Section 2, we describe the basic principle of BOCDR and clarify its difference from that of BOCDA. In Section 3, we present some configurations for improving its performance. In Section 4, we focus on slope-assisted BOCDR and present its principle along with some unique features including the beyond-nominal-resolution effect. In Section 5, we provide a summary and discuss the future prospects of BOCDR technology.

2. Basic Principle of BOCDR

When a light beam is injected into an FUT, it interacts with acoustic phonons, generating backscattered light called Stokes light. This phenomenon is called spontaneous Brillouin scattering. Caused by the exponential decay of the acoustic phonons, the backscattered Brillouin light spectrum, known as BGS, takes the shape of a Lorentzian function with the bandwidth of several tens of megahertz. If the power of the pump light is higher than the Brillouin threshold power $P_{th}$, the Stokes light caused by spontaneous Brillouin scattering acts as a seed of stimulated scattering, and there occurs a transition from spontaneous Brillouin scattering to SBS; as a result, the Stokes light power is drastically enhanced. This transition can be promoted using a so-called pump-probe technique, in which a probe light beam (frequency-downshifted by the BFS) is additionally injected into the other end of the FUT. This is the reason why SBS-based distributed sensor configurations, such as BOTDA, BOFDA, and BOCDA, require light injection into both ends of the FUT.

In Brillouin scattering, whether it is spontaneous or stimulated, the frequency at which the peak power is obtained in the BGS is downshifted by several gigahertz from the incident light frequency, and the amount of this frequency shift is called BFS. In optical fibers, the BFS $\nu_B$ is given by [1]:

$$\nu_B = \frac{2n\nu_A}{\lambda_p},$$  \hspace{1cm} (1)

where $n$ is the refractive index, $\nu_A$ is the acoustic velocity in the fiber, and $\lambda_p$ is the wavelength of the incident pump light. If tensile strain is applied or temperature is changed in a standard silica single-mode fiber (SMF), the BFS shifts to higher frequency in proportion to the applied strain (+480 MHz/%) [3] and the temperature change (+1.18 MHz/K) [4] at 1.55 µm. In some specialty fibers, such as tellurite glass fibers and polymer optical fibers (POFs), it is known that the BFS moves to lower frequency with increasing applied strain (−230 MHz/% [38] and −122 MHz/% [39,40], respectively) and temperature (−1.14 MHz/K [41] and −4.09 MHz/K [39,40], respectively). In both cases, we can derive the strain amplitude and temperature change by measuring the BFS in the fiber.
One of the most essential features of Brillouin-based sensors is their distributed sensing capability. In BOCDR, distributed sensing is achieved using a technique called the synthesis of an optical coherence function (SOCF). The conceptual setup of BOCDR is schematically shown in Figure 1. The optical output from a laser diode is divided into pump and reference light beams. The pump light is injected into the FUT, and the Stokes light is directed into a photodiode (PD). The reference light is used as an optical local oscillator. The electrical beat signal of the two light beams is monitored using an electrical spectrum analyzer (ESA). Since there is a frequency difference of approximately 11 GHz between the Stokes light and the reference light, this configuration is called a self-heterodyne scheme. In order to resolve the position in the FUT, the optical frequency of the laser output is modulated in a sinusoidal waveform by directly modulating the injection current of the laser. From the viewpoint of temporal averaging, the coherence function is synthesized into a series of periodical peaks \( f_m \), of which the period is inversely proportional to the frequency of the sinusoidal modulation \( f_m \). We control \( f_m \) to generate only one correlation peak within the range of the FUT, so that only the Brillouin scattering generated at the position correspondent to the peak has high correlation with the reference light, and then gives high heterodyne output. The peak frequency observed using the ESA gives the BFS caused at the position. By sweeping \( f_m \), the position of the correlation peak is scanned along the FUT, and thus the distribution of the BGS or the BFS is obtained. Note that a delay line is often inserted in the reference path so that the order of the correlation peak in the FUT may not be zero; the 0th-order correlation peak cannot be scanned along the FUT by controlling \( f_m \).

![Figure 1. Conceptual schematic of BOCDR. AC, alternating current; DC, direct current; ESA, electrical spectrum analyzer; FUT, fiber under test; PD, photodiode.](image)

Here, we give another explanation of the operating principle of BOCDR using Figure 2. When the laser frequency is sinusoidally modulated, the frequencies of the reference light and the Stokes light at the PD are expressed by the equations shown in Figure 2, where \( \varphi \) and \( \psi \) are phase factors. While \( \varphi \) is a constant, \( \psi \) changes according to where, in the FUT, the pump light is reflected. For example, when the pump light is reflected at Position A and \( \varphi = \psi + 2 \pi n \) (\( n \): integer), the frequency difference of the reference light and the Stokes light is always the same regardless of time, and so the beat signal can be detected. In contrast, when the pump light is reflected at Position B and \( \varphi \neq \psi + 2 \pi n \), the frequency difference of the two light beams changes according to time, and so the beat signal cannot be observed. From the viewpoint of time averaging, we interpret that a correlation peak is standing at Position A. Now the modulation of the laser frequency is a periodical sinusoidal waveform, these correlation peaks appear periodically along the FUT, so only one correlation peak should be located within the range of the FUT to resolve the position properly, resulting in the limited measurement range. The position of the correlation peak can be scanned along the fiber by adjusting the modulation frequency \( f_m \).
Figure 2. Operating principle of basic BOCDR.

The spatial resolution $\Delta z$ and the measurement range $d_m$ (distance between the neighboring correlation peaks) of BOCDR are given by the same equations as those for BOCDA [25,37]:

$$\Delta z = \frac{v_g \Delta \nu_B}{2\pi f_m \Delta f}, \quad (2)$$

$$d_m = \frac{v_g}{2 f_m}, \quad (3)$$

where $v_g$ is the group velocity of light, $\Delta \nu_B$ is the Brillouin gain bandwidth (~30 MHz) in optical fibers, and $\Delta f$ is the modulation amplitude of the light source. Equation (2) was originally derived for BOCDA, so it is not evident that the spatial resolution of BOCDR is also given by this expression; refer to Reference [37] for the derivation of Equation (2) in BOCDR. According to Equations (2) and (3), it is evident that $\Delta z$ and $d_m$ are in a trade-off relationship, and thus their ratio ($=d_m/\Delta z$) is often used to evaluate the performance of BOCDR. Considering that $\Delta f$ is limited to a half of the BFS, the resolution-to-range ratio of silica-fiber-based BOCDR is limited to 570, which can be extended by some special configurations (refer to the next section). Note that the SNR of BOCDR cannot be simply given as a function of system parameters, such as $\Delta f$, $f_m$, and fiber length.

Finally, we compare the operating principle between BOCDA and BOCDR as shown in Figure 3.

In both systems, the pump light is reflected everywhere in the FUT due to spontaneous Brillouin scattering. In order to resolve the position, in BOCDA, stimulated Brillouin scattering is strongly induced at one specific position in the FUT by injecting the frequency-modulated pump and probe light beams into each end of the FUT. In contrast, in BOCDR, the Stokes light due to spontaneous Brillouin scattering from one specific position in the FUT is selectively observed by the heterodyne detection with the frequency-modulated reference light. As a consequence, the Stokes light from the FUT in one-end-access BOCDR becomes much smaller than that in two-end-access BOCDA. Hence, another point of BOCDR is to utilize the heterodyne detection not only to resolve the position but also to enhance the beat signal.
3. Various Configurations of BOCDR

Since the proposal of BOCDR, numerous special configurations have been developed to enhance its performance. For instance, in order to mitigate the trade-off relationship between the spatial resolution and the measurement range, a temporal gating scheme [42] and a double modulation scheme [43] were developed. In the temporal gating scheme (Figure 4a), the measurement range was extended while maintaining the spatial resolution by exploiting relatively long optical pulses generated using intensity modulators (IMs). Then, we can arbitrarily select a single correlation peak from multiple correlation peaks located in the FUT. In contrast, in the double modulation scheme (Figure 4b), by modulating the optical frequency at two different frequencies simultaneously, the spatial resolution is given by the higher frequency while the measurement range is given by the lower frequency. These techniques can be simultaneously employed.

Figure 4. Special BOCDR configurations with extended measurement ranges. (a) Temporal gating scheme and (b) double modulation scheme. AC, alternating current; DAQ, data acquisition; DC, direct current; DFB-LD, distributed-feedback laser diode; EDFA, erbium-doped fiber amplifier; ESA, electrical spectrum analyzer; FUT, fiber under test; GPIB, general-purpose interface bus; IM, intensity modulator; PC, polarization controller; PD, photodiode; PSCR, polarization scrambler. [42,43]. Copyright (2009,2010) OSA.

 Regarding the polarization, BOCDR was found to have an ability to measure the beat length distribution [44], while the polarization-dependent fluctuations of the Brillouin signals were suppressed by polarization scrambling [45,46]. Some specialty fibers, such as tellurite fibers [38,40], bismuth-oxide fibers [47], and polymer fibers [48], were used in BOCDR to make the most of their special features (high Brillouin gain coefficients, high flexibility, etc.). The influence of a ghost correlation peak was investigated and its suppression was shown to be extremely important [49]. Some simple configurations of BOCDR were developed to further reduce the system cost [50–52]. An apodization scheme based on synchronous intensity modulation [53] and a lock-in detection scheme [54] were also performed to suppress the noise floor and to enhance the strain dynamic range, etc. Finally, to achieve high-speed operation (the sampling rate was limited to <20 Hz in
the standard configuration \cite{55}), phase-detected BOCDR \cite{56–58} and slope-assisted BOCDR were
developed. In both schemes, the idea for high-speed operation is the same; namely, the omission of
the frequency-scanning process for acquiring the BGS. In phase-detected BOCDR, the BGS is converted
from a frequency domain into a time domain and approximated by a one-period sinusoidal waveform,
the phase of which is detected at a high speed. The slope-assisted BOCDR is the main focus of this
paper and will be detailed in the following section.

4. Development of Slope-Assisted BOCDR

In this section, we describe the fundamentals, unique features, and recent advances of the
high-speed configuration of BOCDR, named slope-assisted BOCDR \cite{59–61}, with an emphasis on the
so-called beyond-nominal-resolution effect.

4.1. Principle and Fundamental Operation

In the standard configuration of BOCDR, the BFS at a single sensing point is derived after
acquiring the whole BGS. In contrast, the slope-assisted BOCDR provides the BFS information using
the BGS slope. This idea has been already proposed for BOTDA \cite{62–64}. As depicted in Figure 5a,
the BFS is in one-to-one correspondence with the spectral power $P_{B0}$ at a certain frequency $\nu_{B0}$, which is
set at the high-frequency point in the linear region (lower-frequency side) of the BGS slope. Then, when
the BFS slightly shifts to higher frequency by strain, etc., $P_{B0}$ decreases linearly; when the slight loss
occurs in the FUT, the spectral power of the BGS entirely decreases, also leading to the reduction of
$P_{B0}$.

Even if the BFS change is so large that $\nu_{B0}$ gets out of the linear region, so long as
$P_{B0}$ is in one-to-one correspondence with the BFS, this system operates properly (with a reduced sensitivity) by simple
nonlinear compensation. One may point out that the noise floor of correlation-domain techniques is
influenced by the sidelobes of the correlation peak and that the slope-assisted configuration does not
work properly in principle, but this issue can be mitigated if we accept the deterioration of the spatial
resolution to some extent just in the same manner as in the phase-detected BOCDR \cite{56}.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{slope_assisted_BOCDR.png}
\caption{Schematic illustrations of the operating principle of slope-assisted BOCDR. (a) One-to-one
 correspondence between the BFS and the spectral power $P_{B0}$ at frequency $\nu_{B0}$. The dotted curve is
 the initial BGS, and the solid curve is the BGS shifted to higher frequency because of strain and/or
 heat. (b) $P_{B0}$ distributions along the FUT with (solid curve) and without (dotted line) partial strain
 and heat. (c) $P_{B0}$ distributions along the FUT with (solid curve) and without (dotted line) a point loss.
 Reproduced with permission from \cite{59}. Copyright (2016) IEEE.}
\end{figure}

Figure 5b,c schematically show the changes in the $P_{B0}$ distributions when strain (or heat) and
loss are locally applied, respectively. The strain and temperature effects cannot be separated in this
method, but the loss effect can be discriminated from the locally applied strain (or temperature change)
in most cases, because the decreased $P_{B0}$ value does not return to the initial value. The $P_{B0}$ change
distributions (calculated by substituting the resultant $P_{B0}$ distributions (solid curves) from their initial
distributions (dotted lines)) are used as final measurement data.

To evaluate the optimal $\nu_{B0}$ value and the bandwidth of the linear region, we analyzed a raw BGS
with a BFS of 10.89 GHz (see Figure 6a), which was experimentally obtained when the FUT length
$L$ and experimental conditions (such as the modulation frequency $f_m$ and amplitude $\Delta f$) were set to
the same values as those for the initial experiment ($L = 5.0\ m$, $f_m = 8.0\ MHz$, $\Delta f = 1.4\ GHz$) [59]. Here, we defined the linear region as the region where the change in the BGS slope was suppressed within 20% compared to its maximum. Based on the slope (i.e., differential coefficient) dependence on the frequency (Figure 6b) obtained by differentiating the BGS with respect to frequency, the optimal $\nu_{B0}$ value to widen the linear region was found to be 10.85 GHz. The bandwidth of the linear region was approximately 50 MHz, which corresponds to the strain of up to $\sim 1035\ \mu\varepsilon$ and the temperature change of $\sim 45\ K$. In this linear region, the theoretical strain and temperature dependence coefficients were calculated to be $2.1 \times 10^{-4}\ dB/\mu\varepsilon$ and $4.3 \times 10^{-3}\ dB/K$, respectively.

*Figure 6.* (a) Measured BGS and (b) its differential coefficient at each frequency. The linear region of the lower-frequency side is indicated. Reproduced with permission from [59]. Copyright (2016) IEEE.

The FUT employed in the initial experiment was a 5.0-m-long silica SMF with a BFS of 10.89 GHz at 1.55 $\mu m$ at room temperature. The experimental setup of slope-assisted BOCDR is schematically shown in Figure 7, which is basically the same as Figure 1; the only essential difference lies in the final signal processing. The output light from a distributed-feedback laser diode at 1.55 $\mu m$ was divided into two light beams, pump and reference. The pump light was amplified to $\sim 24\ dBm$ using an EDFA and injected into the FUT. After passing through a $\sim 1\$ km-long delay line and another EDFA (amplified to $\sim 5\ dBm$), the reference light was used for heterodyne detection with the Stokes light, which was amplified to $\sim 2\ dBm$. The polarization-dependent fluctuations were suppressed using a polarization scrambler (PSCR). The heterodyned optical signal was converted into an electrical signal using a PD and was guided to an ESA. Using the narrowband-pass filtering function of the ESA, the $P_{B0}$ change at a fixed frequency $\nu_{B0}$ ($=10.85\ GHz$) was sequentially output to an oscilloscope (OSC).

*Figure 7.* Experimental setup of slope-assisted BOCDR. AMP, amplifier; EDFA, erbium-doped fiber amplifier; ESA, electrical spectrum analyzer; FUT, fiber under test; LD, laser diode; OSC, oscilloscope; PD, photodiode; PSCR, polarization scrambler. Reproduced with permission from [59]. Copyright (2016) IEEE.
In the initial experiment, a 0.1-m-long section around the distal open end of the FUT was bent to suppress the Fresnel reflection. The modulation frequency $f_m$ and amplitude $\Delta f$ were set to 7.975–8.055 MHz and 1.4 GHz, respectively, corresponding to the measurement range of 12.9 m and the theoretical spatial resolution of 88 mm. The repetition rate was 100 Hz, and averaging was performed 16 times on the OSC. The room temperature was 26 °C. The measured results of the fundamental characterization, i.e., the $P_{B0}$ change dependencies on strain, temperature, and loss, are presented in Reference [59] (the data are not presented here because of the low SNR). The strain-, temperature-, and loss-dependence coefficients of the output signal were $1.95 \times 10^{-4}$ dB/µε, $4.42 \times 10^{-3}$ dB/K, and 0.191, respectively. A proof-of-concept demonstration of slope-assisted BOCDR was then performed by simultaneous measurement of strain, temperature, and loss. The structure of the 5.0-m-long FUT is shown in Figure 8a; the ambient temperature was changed to 55 °C along the 1.9–2.1-m section, a 0.64-dB loss was applied at the midpoint, and a 550 µε strain was applied to the 3.5–3.7-m section. Figure 8b shows the measured $P_{B0}$ change distribution along the FUT. The $P_{B0}$ changes corresponding to the temperature change, loss, and strain were observed at the expected sections. The amounts of the $P_{B0}$ changes for the temperature change, loss, and strain were approximately 0.16, 0.14, and 0.12 (=0.26–0.14) dB (corresponding to the temperature change, loss, and strain of ~62 °C, ~0.73 dB, and ~615 µε, respectively). The measurement errors probably originate from the signal fluctuations and the resultant low SNR.

Figure 8. (a) Structure of the FUT. (b) Measured $P_{B0}$ change distribution. Reproduced with permission from [59]. Copyright (2016) IEEE.

4.2. Beyond-Nominal-Resolution Effect

One fundamental issue that must be solved to characterize the slope-assisted BOCDR operation is the correspondence between the final system output (i.e., power-change distribution) and the actual BFS distribution. In standard BOCDR based on frequency information, these two distributions have been proven to be identical in principle; however, in slope-assisted BOCDR based on power information, no report has been made. Here, we theoretically and experimentally show that the final system output of slope-assisted BOCDR is generally different from the actual BFS distribution. We also show that, even when the strained section is shorter than the nominal resolution, some shift in the power change can be observed. This feature is unique to the slope-assisted BOCDR and useful for practical applications.

To start with, we simulated the system output of slope-assisted BOCDR. We assumed that one section of the FUT was uniformly strained. The magnitude of the strain was assumed to constantly lie below the upper limit of the linear region (~2000 µε). The lengths of the strained section were set to $0.25R$, $0.5R$, $0.75R$, $R$, $2R$, $5R$, and $10R$, where $R$ indicates the nominal spatial resolution calculated using Equation (2). First, the simulation results for the strain distributions acquired using the standard
BOCDR (deduced from the BFS distributions using the linear BFS-to-strain relationship) are shown in Figure 9a, which completely reproduce the actual BFS distributions. Next, the simulation results for the strain distributions obtained from the slope-assisted BOCDR (also deduced from the final power-change distributions simply based on the linear power-to-strain relationship) are shown in Figure 9b (strained: $0.5R$, $R$, $2R$, $5R$, and $10R$) and Figure 9c (strained: $0.25R$, $0.5R$, $0.75R$, and $R$). Here, for simplicity, we neglected both the complicated longitudinal shape of the correlation peak and the influence of its sidelobes [65]; that is, the longitudinal shape of the correlation peak was approximated by a rectangular profile with a length of $R$. At the ends of the strained section (i.e., the boundaries between the strained and non-strained sections), the power change varied linearly with the length of $R$; consequently, each whole power-change distribution showed a trapezoidal shape (including triangular). Thus, we see that when the strained section is sufficiently longer than $R$, the power-change distribution almost reproduces the actual BFS distribution. In contrast, when the length of the strained section is approximately $R$ or only a few times longer than $R$, the correct BFS distribution cannot be directly obtained (under the assumption that the strain is uniformly applied; however, the correct information can be easily derived). What is notable here is that, even when the strained section is shorter than $R$, we can observe a trapezoidal-shaped shift in the power change and thereby obtain the information that some irregularity has occurred at that point. For instance, when the length of the strained section is $0.5R$, a trapezoidal shape with a maximal power-change shift (corresponding to half the amount obtained with a strained section longer than $R$) is observed.

![Figure 9](image_url). Deduced strain distributions directly obtained from the final power outputs of (a) standard BOCDR and (b,c) slope-assisted BOCDR. Note that the traces in (a) give the correct strain distributions. Reproduced with permission from [60]. Copyright (2016) OSA.

Subsequently, the aforementioned simulation results including this “beyond-nominal-resolution” effect are experimentally verified (note that with this effect, we cannot distinguish two hot spots of which the distance is smaller than the nominal resolution, as the two hot spots are broadened; we can just detect an extremely short hot spot, and in this meaning, the spatial resolution of the system is not enhanced with this effect). The setup was basically the same as that in Figure 7; the change in the spectral power at 10.81 GHz was sequentially output to the OSC (owing to the difference in the video bandwidth of the ESA). The FUT was a 13.0-m-long silica SMF with a BFS of 10.86 GHz at 1.55 µm at room temperature (25 °C). Measurements were performed using two configurations: one for a relatively high spatial resolution and the other for a relatively low resolution (required to
investigate the beyond-nominal-resolution effect). In the first configuration with a high resolution, strains of 750 με and 1500 με were applied to 5-cm-, 10-cm-, 20-cm-, 50-cm-, and 100-cm-long sections of the FUT, as depicted in Figure 10a. The modulation frequency $f_m$ and amplitude $\Delta f$ were set to 7.11–7.31 MHz and 1.3 GHz, respectively, corresponding to the measurement range of 14.5 m and the theoretical spatial resolution of 9.5 cm according to Equations (2) and (3). In the second configuration with a low resolution, a strain of 1500 με was applied to 5-cm-, 10-cm-, 15-cm-, and 20-cm-long sections of the FUT (see Figure 10b). The modulation frequency $f_m$ was swept in the same range (7.11–7.31 MHz), thus giving the same measurement range (14.5 m). The modulation amplitude $\Delta f$ was reduced to 0.7 GHz, corresponding to a theoretical spatial resolution of 19.6 cm. In both configurations, the repetition rate was set to 100 Hz, and averaging was performed 64 times on the OSC to improve the SNR.

First, we present the experimental results with a relatively high spatial resolution (9.5 cm). An example of the measured power change distribution (converted into strain) along the whole length of the FUT (with a 1500 με strain applied to a 20-cm-long section) is shown in Figure 11a. At this scale, it appears that the correct amount of strain was detected at the correct location. The strain distributions measured when strains of 750 με and 1500 με were applied (magnified views around the strained sections), simply deduced from the power-change distributions based on the linear power-to-strain relationship, are shown in Figure 11b,c, respectively. Each distribution is shifted by 3000 με, and the simulated data are indicated by dotted lines. The trends in the measured distributions agree well with the simulation results, including the case where the strained section is half the nominal spatial resolution. This indicates that our relatively rough simulation is almost sufficient to predict the experimental results, which is beneficial from the viewpoint of simulation cost.

We then performed similar experiments with a relatively low spatial resolution (19.6 cm) to evaluate the beyond-nominal-resolution effect. The magnified views of the strain distributions (simply deduced from the power-change distributions), measured when a strain of 1500 με was applied, are shown in Figure 12. As the strained section becomes shorter, the maximal power-change shift becomes smaller. The trend in the measured distributions is basically in good agreement with the simulation results. As the strained section is shortened further, the signal is buried by the noise. The standard deviation of the noise floor (power fluctuations corresponding to the strain of the non-strained sections) was calculated to be approximately 130 με in this measurement. This amount is theoretically obtained as the maximal strain when the strained section is 1.7 cm, which could be regarded as the shortest detectable length. Note that this value is influenced by various experimental parameters such as the amount of the actual strain, the number of averaging, the incident power, etc., the details of which are described in the following subsection.
Figure 11. Deduced strain distributions with a spatial resolution of 9.5 cm: (a) example measurement along the whole length of the FUT when a 1500 με strain was applied to a 20-cm-long section, and magnified views when strains of (b) 750 με and (c) 1500 με were applied to 5-cm- to 100-cm-long sections. In (b,c), each distribution was shifted by 3000 με, and the dotted lines indicate the simulated data. Reproduced with permission from [60]. Copyright (2016) OSA.

Figure 12. Magnified views of the deduced strain distributions with a spatial resolution of 19.6 cm; a 1500 με strain was applied to 5-cm- to 20-cm-long sections. Each distribution was shifted by 3000 με, and the dotted lines indicate the simulated data. Reproduced with permission from [60]. Copyright (2016) OSA.

4.3. Detection of Extremely Short Hot Spots

Here, we performed more detailed characterization of the beyond-nominal-resolution effect of slope-assisted BOCDR. First, using a silica SMF, we found that a strained section which is over 50 times
shorter than the nominal spatial resolution can be detected. Then, we showed the usefulness of the beyond-nominal-resolution effect by detecting a 2-mm-long strained section along a silica SMF and a 5-mm-long heated section along a POF. These values are smaller than the world records previously reported, which are 3 mm [66] and 100 mm [67] for a silica SMF and a POF, respectively.

First, to characterize the beyond-nominal-resolution effect, we employed a 14.0-m-long silica SMF as an FUT. The output light from a laser was amplified to ~25 dBm using an EDFA and injected into the FUT. The BFS of the FUT was 10.89 GHz at 1.55 \( \mu \)m at 26 °C (room temperature). The open end of the FUT was bent to suppress the Fresnel reflection. The spectral power-change at 10.87 GHz (determined by differentiating the BGS) was monitored using an OSC. The modulation amplitude \( \Delta f \) and the modulation frequency \( f_m \) were set to 0.19 GHz and 5.10–5.26 MHz, respectively, leading to the nominal spatial resolution of 1.01 m and the measurement range of 20.1 m. A strain of 0.1% was applied to 0.01-, 0.02-, 0.05-, 0.10-, 0.20-, 0.50-, and 1.00-m-long sections of the FUT, as shown in Figure 13a. When the length of the strained section was changed, the position of its proximal end was fixed. Averaging was performed 512 times on the OSC.

Subsequently, exploiting the beyond-nominal-resolution effect, we attempted to detect the shortest-ever strained and heated sections along a silica SMF and a POF. In this experiment, we injected ~28 dBm light to the FUTs to enhance the measurement sensitivity, and averaging was performed 1024 times. To begin with, we employed a 2.0-m-long silica SMF as an FUT, the BFS of which was 10.85 GHz at room temperature. We applied strains of 0.10, 0.15, and 0.20% to a 2-mm-long section (~55 times shorter than the nominal spatial resolution; see below), as depicted in Figure 13b. The nominal spatial resolution and the measurement range were 0.11 m and 7.64 m (\( \Delta f \): 0.67 GHz; \( f_m \): 13.45–13.54 MHz), respectively. The change in the spectral power at 10.84 GHz was observed using the OSC. Then, a 2.0-m-long perfluorinated graded-index POF [39, 68, 69] (core diameter: 50 \( \mu \)m; propagation loss at 1.55 \( \mu \)m: 0.25 dB/m; BFS at room temperature: 2.75 GHz) was used as an FUT. A 5-mm-long section was heated to 35, 45, and 55 °C (see Figure 13c). The modulation amplitude \( \Delta f \) and the modulation frequency \( f_m \) were set to 0.69 GHz and 24.70–24.84 MHz, respectively, resulting in the nominal spatial resolution of 0.21 m and the measurement range of 4.5 m. Note that the length of the heated section was over 40 times shorter than the nominal spatial resolution. The change in the spectral power at 2.78 GHz was monitored.

![Figure 13](image)

**Figure 13.** (a) Structure of a silica SMF under test. The length of the strained section \( L_\varepsilon \) was set to 0.01, 0.02, 0.05, 0.10, 0.20, 0.50, and 1.00 m. (b) Structure of a silica SMF under test, which was locally strained for 0, 0.10, 0.15, and 0.20%. (c) Structure of a POF under test, which was locally heated to 26, 35, 45, and 55 °C. Reproduced with permission from [61]. Copyright (2016) JSAP.

The power-change distributions measured when the length of the strained section \( L_\varepsilon \) was reduced from 1.00 m to 0.01 m are shown in Figure 14a. Note that the nominal spatial resolution was 1.01 m.
throughout the measurement. The vertical axis was normalized so that the maximal power-change became 1 when $L_ε$ was 1.00 m. Each distribution was displayed with a vertical interval of 0.5. When $L_ε$ was 1.00 m, the power-change distribution showed a triangular shape. As $L_ε$ decreased, the maximal power-change also decreased. When $L_ε$ was 0.02 m, the power-change was still clearly detected, but it became almost comparable to the signal fluctuations when $L_ε$ was 0.01 m. Thus, in this experimental condition, a strained section, which was over 50 times shorter than the nominal spatial resolution, was shown to be detectable. Figure 14b shows the normalized maximal power-change plotted as a function of $L_ε$. The error bars were standard deviations of the signal fluctuations at non-strained sections. The maximal power-change decreased almost linearly with decreasing $L_ε$, which agrees well with the theory. The observed length of non-zero-power-change section was almost equal to the sum of the strained length $L_ε$ and the nominal spatial resolution, which also agrees with the theory.

![Figure 14](image)

**Figure 14.** (a) Normalized power-change distributions measured when the length of the strained section $L_ε$ was reduced from 1.00 m to 0.01 m; each distribution was shifted by 0.5. Dotted lines indicate the theoretical trends. (b) Maximal power-changes plotted as a function of $L_ε$. The error bars were calculated as standard deviations of the signal fluctuations at non-strained sections. The dotted line is a linear fit. The inset shows the magnified view at $L_ε$ shorter than 0.1 m. Reproduced with permission from [61]. Copyright (2016) JSAP.

Finally, exploiting the beyond-nominal-resolution effect verified above, we attempted to detect the shortest-ever strained and heated sections along a silica SMF and a POF. Figure 15a shows the normalized power-change distributions measured when the strain of 0.10, 0.15, and 0.20% were applied to a 2-mm-long section of the silica SMF. The local power-changes corresponding to the strain were observed at the correct position. The lengths of the power-changed sections appeared to be much longer than 2 mm; in theory, they should be almost the same as the nominal resolution (0.11 m), which moderately agrees with the measured results. The maximal normalized power-change of each distribution in Figure 15a was plotted as a function of applied strain in Figure 15b. With increasing strain, the power-change also increased almost linearly, which indicated the magnitude of the strain can be correctly measured in this strain range. Then, we performed a similar experiment using the POF. The normalized power-change distributions measured when the 5-mm-long section was heated to 26 (room temperature), 35, 45, and 55 °C are shown in Figure 16a. The abrupt power-changes were observed at the correct position along the POF. The lengths of the power-changed sections moderately
agreed with the nominal resolution (0.21 m). The magnitude of the maximal power-change was in proportion to the temperature change, as shown in Figure 16b, indicating the potential feasibility of distributed temperature sensing.

**Figure 15.** (a) Normalized power-change distributions along a silica SMF measured at four strains. (b) Maximal power-changes plotted as a function of strain. The dotted line is a linear fit. Reproduced with permission from [61]. Copyright (2016) JSAP.

**Figure 16.** (a) Normalized power-change distributions along a POF measured at four temperatures. (b) Maximal power-changes plotted as a function of temperature. The dotted line is a linear fit. Reproduced with permission from [61]. Copyright (2016) JSAP.

4.4. Other Achievements

In addition to the detection of the extremely short hot spots using the beyond-nominal-resolution effect, a number of remarkable advances have been made in the slope-assisted BOCDR. First, by analyzing the BGS shape, the measurement sensitivity dependencies on the incident power and the spatial resolution were investigated [70]. The sensitivity was shown to be enhanced with higher incident power and/or lower spatial resolution; this result was verified through distributed temperature measurements. Then, we implemented slope-assisted BOCDR using a high-loss POF [71]. Owing to the gradual reduction in the transmitted power along the POF, the measurement sensitivities were found to depend on the sensing position. This unique effect was investigated experimentally, and a correct POF-based distributed measurement was performed by compensating this effect. We also demonstrated loss-insensitive operation by employing a special silica fiber with low bending loss [72]. We measured the coefficients of the power-change dependencies on strain and temperature, and by comparing the distributed strain and temperature measurement results using a standard silica fiber and the special fiber, showed that this configuration offers highly stable loss-insensitive operation. Another advance was made from a more practical viewpoint; we presented an example of diagnosis using a composite structure with carbon fiber-reinforced plastics [73]. A silica SMF was embedded in this composite structure during a vacuum-assisted resin transfer molding process. When the composite structure was bent, the system output agreed well with the actual compressive and tensile strain...
distributions. We were also able to detect the breakage of the embedded fiber, which indicated that the slope-assisted system is potentially beneficial for structural health monitoring. In addition, very recent advances include the enhancement of the stability and strain sensitivity using polarization-maintaining fibers [74] and the demonstration of the beyond-nominal-resolution effect with a long measurement range of over 10 km.

5. Conclusions

We reviewed the BOCDR technology from the basic principle to the recent advances. In Section 1, a variety of Brillouin-based distributed sensing techniques including BOCDR and BOTDA were introduced. In Section 2, the basic operating principle of BOCDR was presented. In Section 3, some configurations for improving the performance of BOCDR were described. In Section 4, the slope-assisted BOCDR was detailed; the operating principle and some unique features including the beyond-nominal-resolution effect were presented. Thus, significant technical advances have been achieved to enhance the performance of BOCDR. However, there still remain some important issues to be tackled. One unclarified point of this system is the measurement accuracy, which should be in a trade-off relationship with some parameters such as an average count (or measurement time), spatial resolution, incident optical power, etc. Full investigation of the measurement accuracy is extremely important in order for users to judge whether BOCDR can be employed or not for their purposes. Another point is the clarification of the maximal sampling rate, which is currently limited by the electronic devices used in the setup (in any configuration of BOCDR). The measurement instability caused by the power fluctuations is also a problem in the slope-assisted configuration, which could be mitigated using the ratio between the spectral powers at two frequencies; this push-pull scheme will provide another configuration for loss-insensitive operation. In addition, the dynamic range of slope-assisted BOCDR currently limited by the BGS shape could be extended by low-pass filtering the spectrum (at the cost of the sensitivity). Brillouin-based distributed sensing is, in general, constantly confronted with a problem of discriminative sensing of strain and temperature, and BOCDR is no exception. Combined use of some other sensing mechanisms [75–84] will be necessary. Finally, the current setup is not suitable for field tests outside the laboratory. The system portability should be improved by implementing the functions of the relatively large devices, such as the ESA, the EDFAs, the PSCR, and the frequency-modulated laser, using local electronic circuits and/or module-type devices. These replacements will also lead to reduction in the system cost. We hope that BOCDR will, in the near future, serve as one of the most promising Brillouin-based distributed sensing techniques for practical applications because of its single-end accessibility and many other advantages.

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