Measurement range enlargement in Brillouin optical correlation-domain reflectometry based on double-modulation scheme

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Abstract: We have demonstrated a double-modulation scheme to enlarge the measurement range of Brillouin optical correlation-domain reflectometry for fiber-optic distributed strain sensing. In this scheme, the frequency of the laser output is simultaneously modulated with two different frequencies. In the experiment, 53-cm resolution and 1.5-km measurement range were simultaneously obtained. Furthermore, 27-cm resolution and 1.5-km measurement range were also simultaneously achieved when a noise-floor compensation technique was employed.

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References and links
1. Introduction

Among various kinds of fiber-optic sensors, Brillouin optical correlation-domain reflectometry (BOCDR) [1] has the capacity to measure the distribution of strain and/or temperature along a fiber under test (FUT) from a single end. So far, 13-mm spatial resolution has been obtained in a silica fiber [2], which is the best result ever reported in spontaneous Brillouin scattering-based reflectometers. However, BOCDR suffers from a trade-off between the measurement range and the spatial resolution. Their ratio \( N_R \) is fixed at approximately 570 due to the limitation caused by Rayleigh scattering-induced noise [1]. For example, when the spatial resolution is set to 40 cm or 13 mm, the measurement range becomes 224 m [1] or 7.6 m [2], respectively. Thus, in order to achieve kilometer-order measurement range, the resolution must be 2 m or larger, which is even worse than that of basic time-domain techniques (~1 m [3]), such as Brillouin optical time-domain reflectometry (BOTDR) [4] and Brillouin optical time-domain analysis (BOTDA) [5]. In the time-domain systems, some progress has also been made to enhance the resolution [6]-[7].

To obtain higher \( N_R \), a temporal gating scheme was implemented [8], where any correlation peak within the FUT can be arbitrarily selected by a time-domain technique. In the experiment, 66-cm resolution and 1-km measurement range were simultaneously achieved. The ratio \( N_R \) was 1515, which is about three times as high as that of the basic BOCDR. However, the signal-to-noise (S/N) ratio was so low that \( N_R \) could not be enhanced further.

In the case of Brillouin optical correlation-domain analysis (BOCDA) systems [9], a multiple-modulation scheme is known to be an alternative method to obtain higher \( N_R \) [10], where the frequency of the laser output is simultaneously modulated with multiple different frequencies. In the previous experiment, by modulating the laser output at \( 2f_0 \) and \( 3f_0 \) simultaneously (where \( f_0 \) is a fundamental frequency), \( N_R \) was enhanced by three times.

In this paper, we demonstrate a double-modulation scheme to enlarge the measurement range of BOCDR while maintaining the spatial resolution. The optimized modulation parameters are described, such as the combination of the frequencies to be used, and their amplitudes. Then, the operating principle of the scheme is theoretically analyzed and simulated. In the experiment, a strain-applied 90-cm section is successfully detected with 53.1-cm resolution and 1.51-km measurement range (\( N_R = 2845 \)). Moreover, a strain-applied 40-cm section is also detected with 26.5-cm resolution and 1.51-km measurement range (\( N_R = 5690 \)) by the use of a noise-floor compensation technique.

2. Principle

Spontaneous Brillouin scattering occurs when light is Bragg-reflected by the refractive index modulations produced by acoustic phonons. Since the phonons decay exponentially, the backscattered Brillouin light (Stokes light) spectrum, also known as Brillouin gain spectrum (BGS), takes the shape of a Lorentzian function [11]. The Stokes light suffers a Doppler shift called Brillouin frequency shift (BFS), which depends on tensile strain and temperature change applied to the optical fiber. For example, in a standard silica single-mode fiber (SMF), BFS of about 11 GHz slightly varies to higher frequency in proportion to the applied strain and the temperature change with coefficients of 0.058 MHz/\( \mu \varepsilon \) [12] and 1.18 MHz/K [13], respectively. Hence, BFS can provide the information on the magnitude of strain and temperature change in the fiber.

BOCDR [1] is a technology to measure the distribution of strain and/or temperature along an FUT from a single end, based on the correlation control of continuous lightwaves. The Stokes light due to the spontaneous Brillouin scattering of the pump light in the FUT is heterodyned with the reference light (self-heterodyne). In order to resolve the strain-applied position, the pump light and the reference light are sinusoidally frequency-modulated, producing periodical correlation peaks along the FUT. The measurement range \( d_m \), that is, the interval of the correlation peaks, and the spatial resolution \( \Delta z \) are given by:
respectively, where \( c \) is the velocity of light, \( n \) the refractive index, \( f_{\text{mod}} \) the modulation frequency of the light source, \( \Delta v_B \) the Brillouin gain bandwidth in optical fibers, and \( \Delta f \) the modulation amplitude of the light source. The number of effective sensing points \( N_R \), which can be regarded as the evaluation parameter of the system, is given by the ratio between \( d_m \) and \( \Delta z \), as:

\[
N_R = \frac{d_m}{\Delta z} = \frac{\pi \Delta f}{\Delta v_B}.
\]

According to Eq. (3), \( \Delta f \) needs to be increased to obtain higher \( N_R \). Although \( \Delta f \) is not limited in BOCDA [14], \( \Delta f \) must be lower than a half of BFS in the fiber in BOCDR [1], which results in \( N_R \) lower than about 570 for standard silica fibers.

Another way to achieve higher \( N_R \) is to utilize multiple intervals of the correlation peaks. In this case, we select only one correlation peak for a distributed measurement, but suppress other peaks to avoid the crosstalk. Therefore, the measurement range is multiplied while the spatial resolution is maintained. Along with the temporal gating scheme [8], the double-modulation scheme is an effective method for this purpose, and was applied to BOCDA [10].

The experimental setup of BOCDR based on the double-modulation scheme is depicted in Fig. 1. The roles of each device including the polarization scrambler (PSCR) and the optical filters are the same as described in [15]. The pump light and the reference light are sinusoidally frequency-modulated with two different frequencies, \( f_0 (\pm f_c) \) and \( m f_0 \), where \( f_0 \) is a fundamental frequency, \( m \) is an integer, and \( f_c (\sim 0.5 \text{ kHz}) \) is needed to avoid beating between the two frequencies, which causes large fluctuations of BGS. The amplitude of the frequency modulation at \( f_0 \), denoted as \( \Delta f_{m0} \), is set to be several hundreds of MHz (difficult to measure accurately due to the frequency characteristics of the laser circuit). The amplitude at \( m f_0 \), denoted as \( \Delta f_m \), is about 5.4 GHz (a little lower than a half of BFS in silica fibers). Then, as shown in Fig. 2, the spatial resolution is determined by \( m f_0 \), while the correlation peaks of which the orders are not multiples of \( m \) are suppressed by \( f_0 \). Since the modulation at \( f_0 \) does not influence on the resolution due to the low \( \Delta f_c \), it becomes possible to achieve the spatial...
resolution determined by $m f_0$ and the measurement range determined by $f_0$ simultaneously, leading to a larger $N_R$ by $m$ times.

3. Theoretical analysis and simulation

The operating principle of the double-modulation scheme was theoretically analyzed. The frequency modulation of the laser output is represented as Eq. (4):

$$f(t) = f_c + \Delta f_n \sin(2\pi mf_c t) + \Delta f_s \sin(2\pi f_s t),$$ (4)

where is the center frequency. Then, the electric field of the laser output is expressed as Eq. (5):

$$E(t) = \exp\{-j\Phi(t)\},$$ (5)

where $\Phi(t)$ is defined by Eq. (6):

$$\Phi(t) = \int_0^T 2\pi f \left(t, t'ight) dt'.$$ (6)

It is known that the optical coherence function, which is the shape of the correlation peaks along the FUT, is given by the Fourier transform of the spectral density of the light source, or in other words, the autocorrelation function of the electric field of the light source [16]. Therefore, the absolute value of the optical coherence function is calculated as

$$|\psi(\tau_s)| = \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{T/2} \exp\{-j\Phi(t)\} \exp\{j\Phi(t - \tau_s)\} dt,$$

$$= \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{T/2} \exp\left\{-2\pi f_c \tau_s + \frac{2 \Delta f_n}{m f_c} \sin(\pi m f_c \tau_s) \sin\left(2\pi m f_c \left(t - \frac{\tau_s}{2}\right)\right)\right\}$$

$$+ \frac{2 \Delta f_s}{f_c} \sin(\pi f_s \tau_s) \sin\left(2\pi f_s \left(t - \frac{\tau_s}{2}\right)\right)\right\} dt,$$

$$= \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{T/2} \sum_{n=-\infty}^{\infty} \frac{2 \Delta f_n}{m f_c} \sin(\pi m f_c \tau_s) \exp\left\{j2\pi m f_c \left(t - \frac{\tau_s}{2}\right)\right\}$$

$$\cdot \sum_{q=-\infty}^{\infty} \exp\left\{j2\pi q f_s \left(t - \frac{\tau_s}{2}\right)\right\} dt,$$

$$= \lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{T/2} \sum_{n=-\infty}^{\infty} \frac{2 \Delta f_n}{m f_c} \sin(\pi m f_c \tau_s) \exp\left\{j2\pi m f_c \left(t - \frac{\tau_s}{2}\right)\right\}$$

$$\cdot \sum_{q=-\infty}^{\infty} \exp\left\{j2\pi q f_s \left(t - \frac{\tau_s}{2}\right)\right\} dt.$$
\[
\lim_{T \to \infty} \frac{1}{T} \int_{-T/2}^{T/2} \sum_{p=-\infty}^{\infty} \sum_{q=0}^{\infty} J_p \left( \frac{2 \Delta f}{mf_0} \sin \left( \pi mf_0 \tau_q \right) \right) \cdot J_q \left( \frac{2 \Delta f}{f_0} \sin \left( \pi f_0 \tau_q \right) \right) \cdot \exp \left\{ j2\pi \left( \mu m + q \right) f_0 \left( t - \frac{\tau_q}{2} \right) \right\} dt
\]
\[
= \sum_{p=0}^{\infty} J_p \left( \frac{2 \Delta f}{mf_0} \sin \left( \pi mf_0 \tau_1 \right) \right) \cdot J_{-p} \left( \frac{2 \Delta f}{f_0} \sin \left( \pi f_0 \tau_1 \right) \right),
\]
where \( \tau_1 \) is the time delay and \( J_p(x) \) is the \( p \)-th Bessel function of the first kind. When \( m >> 1 \), Eq. (7) is approximately equal to Eq. (8):
\[
\left\| \psi (\tau_0) \right\| \approx \left| J_0 \left( \frac{2 \Delta f}{mf_0} \sin \left( \pi mf_0 \tau_0 \right) \right) \right| \left| J_{-1} \left( \frac{2 \Delta f}{f_0} \sin \left( \pi f_0 \tau_0 \right) \right) \right|,
\]
which shows that the synthesized coherence function in the double-modulation scheme is roughly given by the product of the coherence functions synthesized into a series of periodical delta-function-like peaks by each modulation frequency.

Based on Eq. (7), we simulated the synthesized coherence function when \( m = 4 \), as shown in Figs. 3(a)-3(c). The ratio of the modulation amplitudes \( (\Delta f_5 / \Delta f_1) \) was set to 10. In Fig. 3(c), the 1st, 2nd, 3rd, 5th, 6th, 7th, and 9th correlation peaks were suppressed, which shows that the measurement range was multiplied by 4 times while maintaining the spatial resolution.

![Fig. 3](image_url)

**Fig. 3.** Synthesized coherence functions with the modulation at (a) \( f_0 \) only, (b) \( 4f_0 \) only, and (c) \( f_0 \) and \( 4f_0 \).

### 4. Experiments

First, the effectiveness of the double-modulation scheme was experimentally shown. As the two modulation frequencies, \( f_0 \) and \( 5f_0 \) were used \( (\Delta f_5 = 5.4 \text{ GHz}) \), where \( f_0 \) was set to 68.481 kHz. According to Eqs. (1) and (2), the spatial resolution and the measurement range determined by the conventional single modulation at \( 5f_0 \) were 53.1 cm and 302.1 m, respectively. An SMF of 1 km was used as the FUT, and about 0.15-\% strain was applied to a 3-m section \( (990 - 993 \text{ m}) \). The correlation peak was placed at the middle of the strain-applied section. The polarization state was optimized by adjusting polarization controllers so that the peak intensity of BGS without strain applied becomes maximal. Averaging was conducted 10 times to measure one BGS.
Figure 4(a) shows the measured BGS with and without strain applied when the single modulation at $5f_0$ was applied. Since there were three correlation peaks within the FUT, the change of BGS was not observed as a clear shift of the peak. Here, a kink observed at 10.9 GHz was caused by range switching of the electrical spectrum analyzer (ESA). In contrast, Fig. 4(b) shows the measured BGS when the double-modulation scheme was employed. The applied strain was observed as a clear shift of the BGS peak. The remaining peak at about 10.86 GHz in the curve with strain applied, which can be regarded as noise, originates from the correlation sidelobes that were not completely suppressed. As long as this remaining peak is lower in power than the BGS peak, the measurement is performed correctly. In practical cases with two or more strains applied along the FUT, the power of the remaining peak becomes even smaller.

Then, the double modulation and the single modulation were compared in a distributed strain measurement. A strain of 0.15% was applied to a 90-cm section (990.0 – 990.9 m). With $f_0$ swept from 68.362 kHz to 68.497 kHz, BGS was measured every 5 cm. The other conditions were the same as those in the preceding experiment. The measured distributions of BGS and BFS with the single modulation at $5f_0$ ($m = 5$) are shown in Figs. 5(a) and 5(b), respectively. Although BGS slightly changed at the strain-applied section, a correct distribution of BFS was not acquired. On the other hand, the measured results in the double-modulation scheme with $f_0$ and $5f_0$ are shown in Figs. 6(a) and 6(b). The strain-applied 90-cm section was correctly detected. The measurement accuracy in this experiment was about +/- 7 MHz, corresponding to about +/- 120 µε. The ratio $N_R$ was 2845 ( = 1.51 km / 53.1 cm), which is much higher than 1515 obtained previously in the temporal gating scheme.
The upper limit of $m$ is determined by noise floor of the ESA, polarization state, FUT length, nonlinear dependence of LD frequency, etc. As $m$ is increased, the S/N ratio is deteriorated due to the following two reasons: (i) the remaining peak (noise) in Fig. 4(b) becomes larger; (ii) the spatial resolution becomes higher, which accompanies the reduction of the BGS signal power. The second reason also deteriorates the measurement accuracy.

Finally, the double-modulation scheme was implemented with $f_0$ and $10f_0$ ($\Delta f = 5.4 \text{ GHz}$) using a noise-floor compensation technique [15]. A strain of 0.15\% was applied to a 40-cm section (990.0 - 990.4 m). With $f_0$ swept from 68.362 kHz to 68.474 kHz, the spatial resolution and the measurement range were 26.5 cm and 1.51 km, respectively, corresponding to $N_R$ of 5690. The measured results are shown in Figs. 7(a) and 7(b). Although the S/N ratio was deteriorated compared to that in Fig. 6, the strain-applied 40-cm section was successfully detected. The measurement accuracy was about $+/- 15 \text{ MHz}$, corresponding to about $+/- 260 \mu \text{e}$. We think further research is needed to enhance the measurement accuracy by employing some methods such as those described in Refs [17]-[18].

5. Conclusion

In this paper, we developed a double-modulation scheme to mitigate the trade-off between the measurement range and the spatial resolution in BOCDR. In the experiment, 53-cm resolution and 1.5-km measurement range were simultaneously obtained. Furthermore, 27-cm resolution and 1.5-km measurement range were also simultaneously achieved when a noise-floor compensation technique was employed. We expect the double-modulation scheme will provide BOCDR with more feasibility as a fiber-optic nerve system in smart materials and structures.
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